

Wireless Sensor Networks

*18th Lecture
10.01.2007*



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Topology Control

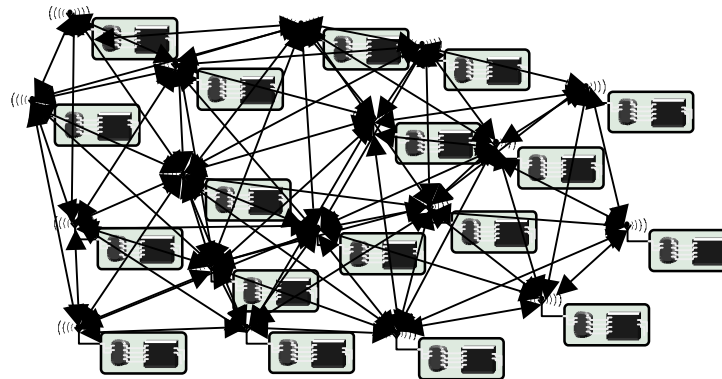
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- **Networks can be too dense – too many nodes in close (radio) vicinity**
- **This chapter looks at methods to deal with such networks by**
 - Reducing/controlling transmission power
 - Deciding which links to use
 - Turning some nodes off



Motivation: Dense networks

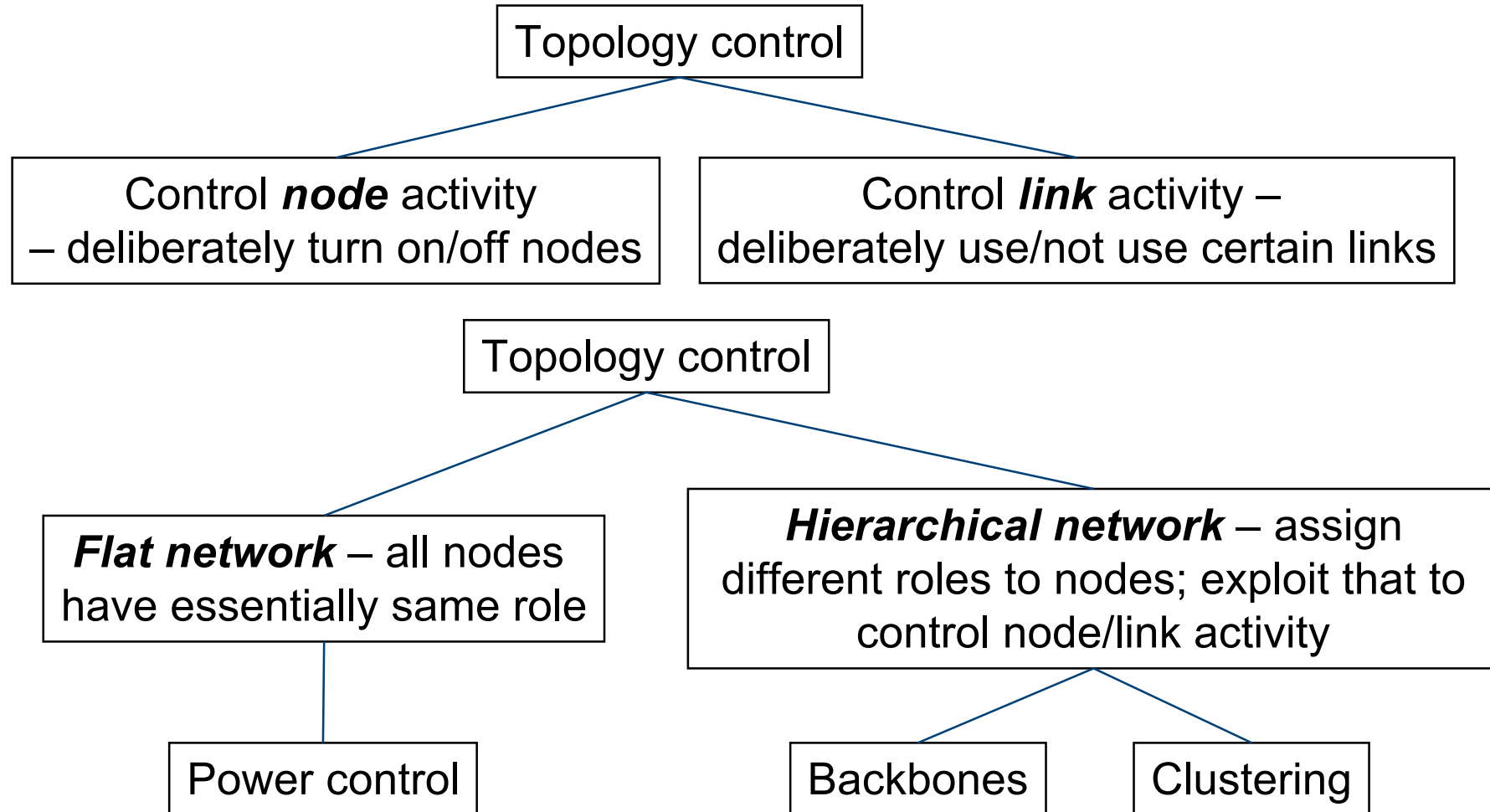
- In a very dense networks, too many nodes might be in range for an efficient operation
 - Too many collisions/too complex operation for a MAC protocol, too many paths to chose from for a routing protocol, ...



- **Idea: Make topology less complex**
 - **Topology:** Which node is able/allowed to communicate with which other nodes
 - Topology control needs to maintain invariants, e.g., connectivity



Options for topology control

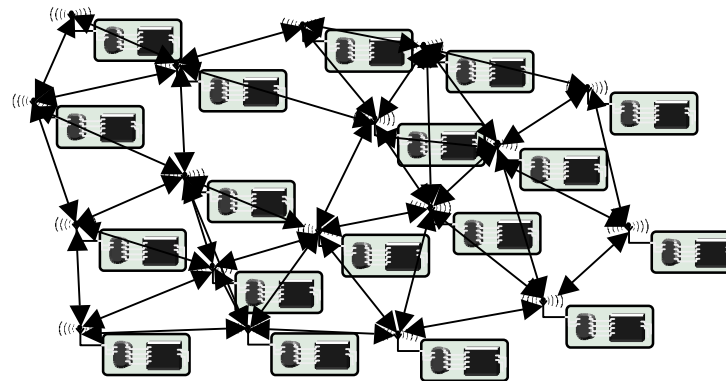




Flat networks

➤ **Main option: Control transmission power**

- Do not always use maximum power
- Selectively for some links or for a node as a whole
- Topology looks “thinner”
- Less interference, ...



➤ **Alternative: Selectively discard some links**

- Usually done by introducing hierarchies



Geometric Spanners with Applications in Wireless Networks

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1. Introduction
 - Definition of Geometric Spanners
 - Motivation
 - Related Work
2. Spanners versus Weak Spanners
3. Spanners versus Power Spanners
4. Weak Spanners versus Power Spanners
 - Weak Spanners are Power Spanners if $\text{Exponent} > \text{Dimension}$
 - Weak Spanners are Power Spanners if $\text{Exponent} = \text{Dimension}$
 - Weak Spanners are not always Power Spanners if $\text{Exponent} < \text{Dimension}$
 - Fractal Dimensions
5. Applications in Wireless Networks
6. Conclusions



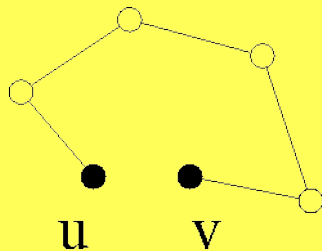
Geometric Spanner Graphs

- A Graph $G = (V, E)$ with $V \subseteq \mathbf{R}^d$ where for all $u, v \in V$ there exists a path $P = (u = u_1, u_2, \dots, u_\ell = v)$ with

limited length:

$$\|P\| := \sum_{i=2}^{\ell} |u_i - u_{i-1}|$$

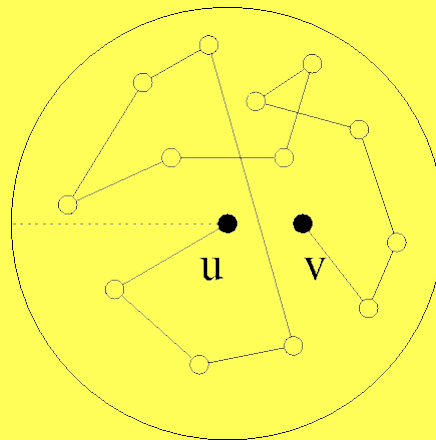
$$\leq c \cdot |u - v|$$



c-Spanner Graph

-in a limited radius:

$$\max_{i=1, \dots, \ell} |u - u_i| \leq c \cdot |u - v|$$

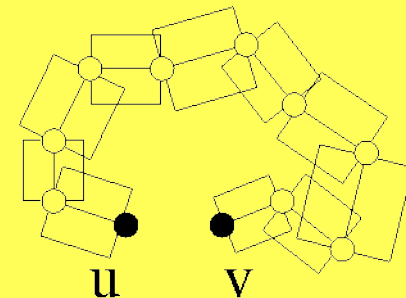


weak c-Spanner Graph

limited energy costs:

$$\|P\|^\delta := \sum_{i=2}^{\ell} |u_i - u_{i-1}|^\delta$$

$$\leq c \cdot |u - v|^\delta$$



(c, δ)-Power-Spanner Graph



Related Work for Spanner Graphs

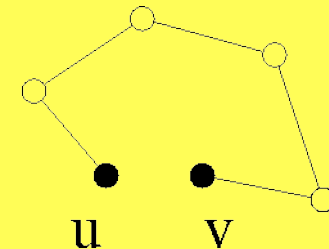
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- **Spanner Graphs introduced by Chew 1986**
- **Peleg & Schaffer first use in Distributed Computing 1989**
- **Applications to**
 - Motion planning [Clarkson 1987]
 - Spanner Trees approximating MST [Yao 1982]
 - Used for FPAS for Traveling Salesman and related problems [Arora et al. 1998]
- **Classic survey of spanners by Eppstein [2000]**

limited length:

$$\|P\| := \sum_{i=2}^{\ell} |u_i - u_{i-1}|$$

$$\leq c \cdot |u - v|$$



c-Spanner Graph



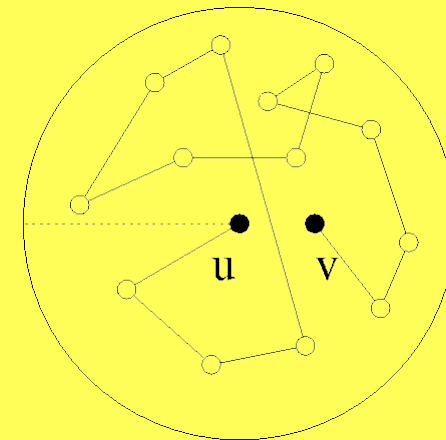
Related Work for Weak Spanners

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- **Applications in geometric searching and**
- **Constructions for spanners and weak spanners with arbitrary approximation ratio (stretch factor) by**
 - Fischer, Meyer auf der Heide, Strothmann 1997
 - Fischer, Lukovszki, Ziegler 1998
- **Optimization of routing time in wireless networks**
 - Grünewald, Lukovski, S., Volbert 2002
 - Jia, Rajaraman, Scheideler 2003
- **Constructions benefitting from locality properties for ad-hoc routing networks**
 - Li, Wan, Wang 2001
 - Grünewald, Lukovski, S., Volbert 2002
 - Wang, Li 2002
 - Wang, Li, Wan, Frieder 2002

-in a limited radius:

$$\max_{i=1,\dots,\ell} |u - u_i| \leq c \cdot |u - v|$$



weak c-Spanner Graph



Related Work for Power Spanners

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➤ Power Spanners used in

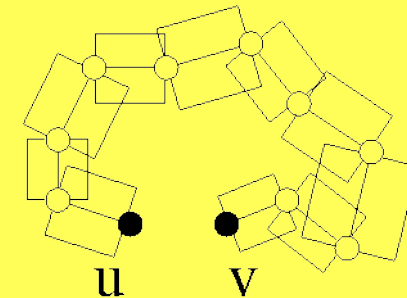
- Grünewald, Lukovszki, S., Volbert 2002
- Li 2003
- Meyer auf der Heide, S, Volbert, Grünewald, 2004

➤ Special cases:

- $\delta = 0$: Hop Spanners,
 - used by Alzoubi et al. 2003
- $\delta = 1$: Power Spanner = Spanner
- $\delta = 2$: Usual Power Spanner
 - (ad hoc networking)
- $\delta > 2$: Energy consumption for messages in reality
 - Rappaport 1996 chooses δ up to 8

limited energy costs:

$$\|P\|^\delta := \sum_{i=2}^{\ell} |u_i - u_{i-1}|^\delta$$
$$\leq c \cdot |u - v|^\delta$$



(c, δ)-Power-Spanner Graph



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Spanners versus Weak Spanners

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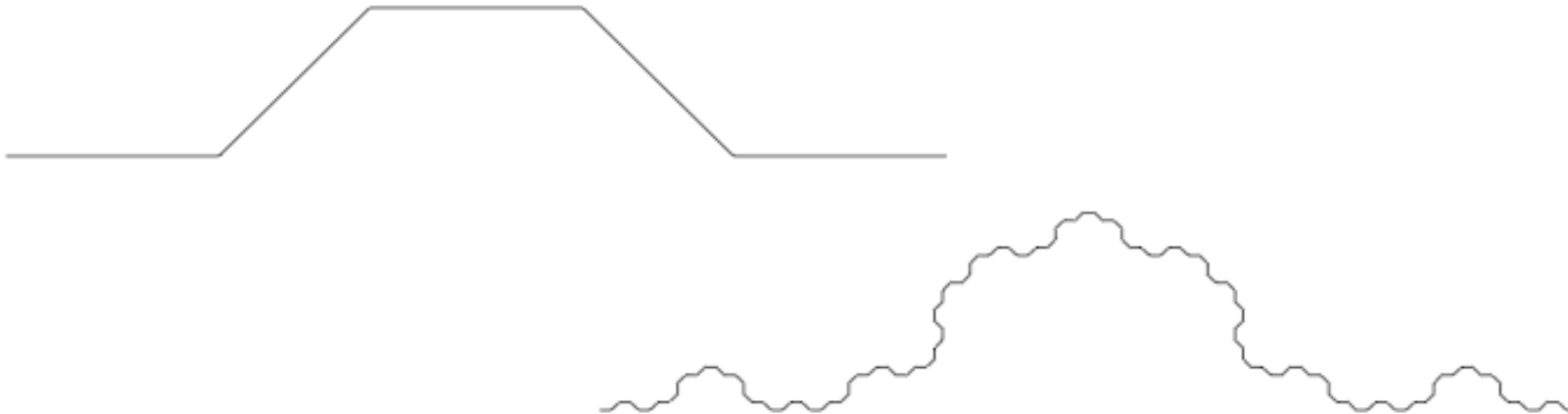
➤ **Fact**

- Every c -Spanner is also a c -Weak Spanner

➤ **Theorem**

- There are Weak Spanner which are no Spanners

➤ **Proof Idea [Eppstein]: use fractal construction**



Thank you

*(and thanks go also to **Holger Karl** for providing some slides)*



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